



# Rocket-in-a-Duct Performance Analysis

Steven J. Schneider and Brian D. Reed  
Glenn Research Center, Cleveland, Ohio

## The NASA STI Program Office . . . in Profile

Since its founding, NASA has been dedicated to the advancement of aeronautics and space science. The NASA Scientific and Technical Information (STI) Program Office plays a key part in helping NASA maintain this important role.

The NASA STI Program Office is operated by Langley Research Center, the Lead Center for NASA's scientific and technical information. The NASA STI Program Office provides access to the NASA STI Database, the largest collection of aeronautical and space science STI in the world. The Program Office is also NASA's institutional mechanism for disseminating the results of its research and development activities. These results are published by NASA in the NASA STI Report Series, which includes the following report types:

- **TECHNICAL PUBLICATION.** Reports of completed research or a major significant phase of research that present the results of NASA programs and include extensive data or theoretical analysis. Includes compilations of significant scientific and technical data and information deemed to be of continuing reference value. NASA's counterpart of peer-reviewed formal professional papers but has less stringent limitations on manuscript length and extent of graphic presentations.
- **TECHNICAL MEMORANDUM.** Scientific and technical findings that are preliminary or of specialized interest, e.g., quick release reports, working papers, and bibliographies that contain minimal annotation. Does not contain extensive analysis.
- **CONTRACTOR REPORT.** Scientific and technical findings by NASA-sponsored contractors and grantees.

- **CONFERENCE PUBLICATION.** Collected papers from scientific and technical conferences, symposia, seminars, or other meetings sponsored or cosponsored by NASA.
- **SPECIAL PUBLICATION.** Scientific, technical, or historical information from NASA programs, projects, and missions, often concerned with subjects having substantial public interest.
- **TECHNICAL TRANSLATION.** English-language translations of foreign scientific and technical material pertinent to NASA's mission.

Specialized services that complement the STI Program Office's diverse offerings include creating custom thesauri, building customized data bases, organizing and publishing research results . . . even providing videos.

For more information about the NASA STI Program Office, see the following:

- Access the NASA STI Program Home Page at **<http://www.sti.nasa.gov>**
- E-mail your question via the Internet to **[help@sti.nasa.gov](mailto:help@sti.nasa.gov)**
- Fax your question to the NASA Access Help Desk at (301) 621-0134
- Telephone the NASA Access Help Desk at (301) 621-0390
- Write to:  
NASA Access Help Desk  
NASA Center for Aerospace Information  
7121 Standard Drive  
Hanover, MD 21076



# Rocket-in-a-Duct Performance Analysis

Steven J. Schneider and Brian D. Reed  
Glenn Research Center, Cleveland, Ohio

Prepared for the  
35th Joint Propulsion Conference and Exhibit  
cosponsored by the AIAA, ASME, SAE, and ASEE  
Los Angeles, California, June 20–24, 1999

National Aeronautics and  
Space Administration

Glenn Research Center

Available from

NASA Center for Aerospace Information  
7121 Standard Drive  
Hanover, MD 21076  
Price Code: A03

National Technical Information Service  
5285 Port Royal Road  
Springfield, VA 22100  
Price Code: A03

# ROCKET-IN-A-DUCT PERFORMANCE ANALYSIS

Steven J. Schneider  
Brian D. Reed

National Aeronautics and Space Administration  
Glenn Research Center  
Cleveland, Ohio 44135

## **Abstract**

An axisymmetric, 110 N class, rocket configured with a free expansion between the rocket nozzle and a surrounding duct was tested in an altitude simulation facility. The propellants were gaseous hydrogen and gaseous oxygen and the hardware consisted of a heat sink type copper rocket firing through copper ducts of various diameters and lengths. A secondary flow of nitrogen was introduced at the blind end of the duct to mix with the primary rocket mass flow in the duct. This flow was in the range of 0 to 10% of the primary massflow and its effect on nozzle performance was measured. The random measurement errors on thrust and massflow were within  $\pm 1\%$ . One dimensional equilibrium calculations were used to establish the possible theoretical performance of these rocket-in-a-duct nozzles. Although the scale of these tests was small, they simulated the relevant flow expansion physics at a modest experimental cost. Test results indicated that lower performance was obtained at higher free expansion area ratios and longer ducts, while, higher performance was obtained with the addition of secondary flow. There was a discernable peak in specific impulse efficiency at 4% secondary flow. The small scale of these tests resulted in low performance efficiencies, but prior numerical modeling of larger rocket-in-a-duct engines predicted performance that was comparable to that of optimized rocket nozzles. This remains to be proven in large-scale, rocket-in-a-duct tests.

## **Introduction**

The rocket-based combined-cycle (RBCC) propulsion system is recognized as a promising technology for Earth-to-orbit vehicles<sup>1,2</sup>. These propulsion systems have four modes of operation for the increasing speed regimes of the vehicle. They are: (1) rocket-ejector ramjet, (2) ramjet, (3) scramjet, and (4) rocket-only modes. Many of the advantages of RBCC engines result from certain synergistic benefits that would not occur if the rocket and airbreathing elements operated separately. One of

these benefits is projected to occur in the rocket-only mode of operation at high altitude, when the rocket nozzle flow expands into the engine duct and onto the vehicle afterbody. This flowpath increases the area ratio of the rocket and, therefore, the specific impulse of that mode of operation. This rocket-in-a-duct operation must be considered when optimizing the engine flow path, because a well-designed ramjet or scramjet flow path does not necessarily result in a high efficiency nozzle for the rocket-only mode of operation. Specifically, there are losses in the duct due to the initial

shock formation as the rocket plume interacts with the duct and there is viscous dissipation in long ducts.

Recently, a modeling effort<sup>3</sup> numerically investigated the effect of various parameters on rocket-in-a-duct nozzle performance. These parameters included: rocket exit area ratio ( $\epsilon$ ), duct inlet area to rocket throat area ratio, base bleed or secondary flow, duct exit-to-inlet area ratio, and duct length-to-inlet diameter ratio ( $L/D$ ). Results from this model showed that large free expansion areas at the rocket exit and long ducts decreased performance, while base bleed and larger duct-exit-to-inlet area ratios increased performance. Over the range of parameters investigated, the model predicted nozzle efficiencies from 77 to 95% of theoretical, one-dimensional equilibrium, vacuum performance.

This paper conducted an experimental assessment of these results using a 110 N class rocket firing into a duct. The small size of the test articles was expected to lead to increased viscous losses and lower efficiencies in the experimental data as compared to the analytical study. An understanding of the relevant physics of the nozzle flow was the goal of these tests.

### **Apparatus and Test Procedures**

A sketch of the test configuration is shown in Figure 1. It consisted of a small gaseous hydrogen/gaseous oxygen rocket of area ratio 8, located inside of a circular duct of diameter,  $D$  and length,  $L$ . The flow from the rocket nozzle freely expanded to the diameter of the duct and turned to follow the duct. A secondary flow of gaseous nitrogen was

injected at the base of the rocket near the blind end of the duct. This secondary flow interacted with the free expansion to establish the pressure at the head end of the duct. This flow was predicted to favorably influence the nozzle performance in Reference 3. The entire assembly was mounted on a thrust stand and performance was measured as outlined below.

Five different rocket-in-a-duct configurations were tested as given in Table 1. These consisted of three different free expansions at a constant length to inlet diameter ratio ( $L/D=5$ ) and three different  $L/D$  ratios at a constant free expansion ( $\epsilon=8$  to 23.5). Tests were 4 seconds long to establish steady state pressure at the blind end of the duct. No diverging duct tests were conducted in this series of tests. Secondary flow of gaseous nitrogen, mostly in the range of 0 to 10% of the core rocket flow, was introduced at the blind end of the duct.

### **Test Articles**

The rocket injector used in this study was designed and fabricated by GenCorp Aerojet Propulsion Division under contract to NASA Glenn Research Center as part of the Space Station Freedom low thrust, gaseous hydrogen/gaseous oxygen rocket technology program<sup>4</sup>. It was a 110 N thrust class platelet type injector with inward radial injection of the propellants. Flame holding was achieved by flow around a bluff body attached to the spark plug tip. The tests were conducted at chamber pressures between 483 and 690 kPa with a nominal mixture ratio of 4. The combustion chamber adjacent to the

injector face was protected with 50% fuel film cooling which was mixed into the core flow by a secondary combustion trip ring in a water cooled adapter.

The rocket consisted of a heat sink type copper chamber, shown mounted in the baseline rocket test configuration without a duct in Figure 2. The chamber and throat diameters, given in Table 1, were 2.54 cm and 1.28 cm, respectively. The rocket had a straight conical nozzle with a 15° half angle to an area ratio  $\epsilon=8$ . Various copper ducts were fabricated from commercial tubing for these tests as shown in Figure 3. Their dimensions are given in Table 1. They were larger in diameter than the rocket and had area ratios of 15.2, 23.5, and 33.4 based on rocket throat area. They were mounted on the large flange shown in Figure 2 for the rocket-in-a-duct tests. An assembly tool was used to ensure concentricity of the duct with the rocket during assembly. One of these assemblies is shown mounted on the injector and water-cooled adapter in Figure 4.

## Test Facility and Test Procedures

### Overview

Testing was conducted in Research Combustion Laboratory, Cell 11 (RCL-11) at NASA GRC. RCL-11 is a test facility designed for altitude testing of low thrust gaseous hydrogen (GH<sub>2</sub>)/gaseous oxygen (GO<sub>2</sub>) rockets. The altitude chamber of this test facility is shown in Figure 5. The altitude chamber was 0.91-m in diameter with viewports for optical access. Mechanical access to the research hardware was provided by a roll-back capability on the tank. A two-stage air ejector system provided continuous suction to maintain a 1.4 kPa

pressure in the tank. Rockets were mounted horizontally and fired into a water-cooled diffuser shown in Figure 4, during chamber roll-back. The distance between the diffuser and nozzle exit was manually adjusted by means of a bellows joint for different test configurations. The exhaust was cooled by a water spray and vented out through muffler stacks to the atmosphere.

Data acquisition was provided by an autonomous, programmable, digital system. Readings were continuously scanned for out-of-tolerance conditions during testing. Real-time data reduction was performed for mass flowrates and performance parameters. Data storage was provided by floppy disks and, for selected parameters, by strip charts. More detailed information about the facility systems can be found in Reference 5.

### Thrust Stand

The thrust stand is shown in Figure 6. The thrust stand was capable of making steady-state thrust measurements up to 220 N thrust. The horizontally oriented thrust stand consisted of a mounting plate, a thrust plate, flexures, a 50-lbf measurement load cell, a 50-lbf calibration load cell, and a nitrogen-loaded ram for calibration.

The rocket was attached to the thrust stand by the mounting plate. The mounting plate was fabricated from a low thermal conductivity material (bakelite) to minimize thermal variations that could be induced by the rocket. The mounting plate was supported by two lateral restraints or flexures. Three columns connected the mounting plate to

the thrust plate, which was also supported by two lateral restraints.

Thrust was transmitted from the thrust plate to a load cell. The load cell was not directly connected to the thrust plate, but rather, had a smooth ball at its end, which sat against the thrust plate. This minimized the transmission of side loads to the load cells. A spring-loaded screw was used to maintain contact between the thrust plate and the flexure ball and to preload the measuring load cell. The measuring load cell was aligned axially with the thruster. Pressurized pistons applied a force against the thrust plate to prevent “chattering” of the ball and thrust plate during pressure transients (sea level-to-altitude, altitude-to-sea level) in the tank. The calibration load cell was attached to the ram, whose yoke pushed against the thrust plate during calibration.

Efforts were made to avoid tares on the thrust stand from attachments to the rocket hardware. Propellant lines, water feed lines, and tubing for the pressure transducers were angled into the rocket hardware at 90° and contributed to flexure stiffness. The pressure transducer tubing was also looped. The ignition cable was contained in thin walled, reinforced Tygon tubing, which was attached to one of the columns on the thrust stand.

In-situ thrust calibrations were performed with pressurized propellant lines and at altitude. Calibration loads were applied by the nitrogen-loaded ram, which pushed against the thrust plate, applying loads on the entire thrust stand. A total of 17 points were taken for each calibration, in roughly equally-spaced

increments, going up to approximately 35-lbf simulated thrust, then back down to zero. Typically three thrust calibrations were performed before and after a test series. These calibrations were combined to provide the thrust precision error for that test series. A straight-line fit of the last calibration before testing was used to calculate site thrust. Whenever the test tank was opened, a new set of thrust calibrations was performed.

The nitrogen-loaded ram was also used to apply a simulated load on the thrust stand (approximately 25 lbf), while data was recorded by the digital data acquisition system, as it would during a real test. This was conducted before and after each test series to determine the data acquisition precision error in thrust (explained further in Appendix A).

#### Data Reduction

Ten basic parameters were measured in testing that were used in performance calculations:

$F_{site}$ : the site force as measured by the thrust stand

$P_c$ : chamber static pressure at the injector face

$P_{amb}$ : the ambient pressure in the altitude chamber

$P_{H2,in}$ : the inlet pressure to the hydrogen critical flow venturi

$T_{H2,in}$ : the inlet temperature to the hydrogen critical flow venturi

$P_{O2,in}$ : the inlet pressure to the oxygen critical flow venturi

$T_{O2,in}$ : the inlet temperature to the oxygen critical flow venturi

$P_{N2,in}$ : the inlet pressure to the nitrogen critical flow venturi



$T_{N2,in}$ : the inlet temperature to the nitrogen critical flow venturi

$T_{chamber}$ : rocket chamber material temperature

From these measured quantities and knowledge of the rocket-in-a-duct geometry, the performance parameters of interest can be determined:

Vacuum Force,  $F_{vac} = F_{site} + P_{amb} A_{exit}$

Vacuum force was determined by free body diagram to be the site force plus the ambient pressure times the nozzle exit area.  $A_{exit}$  is the exit area of the duct.

Hydrogen Mass Flowrate,

$$\dot{m}_{H2} = \left[ C_d A_{ven} \Phi_i^* \left( \frac{\Phi^*}{\Phi_i^*} \right) \right]_{H2} \frac{P_{H2,in}}{\sqrt{T_{H2,in}}}$$

Oxygen Mass Flowrate,

$$\dot{m}_{O2} = \left[ C_d A_{ven} \Phi_i^* \left( \frac{\Phi^*}{\Phi_i^*} \right) \right]_{O2} \frac{P_{O2,in}}{\sqrt{T_{O2,in}}}$$

Nitrogen Mass Flowrate,

$$\dot{m}_{N2} = \left[ C_d A_{ven} \Phi_i^* \left( \frac{\Phi^*}{\Phi_i^*} \right) \right]_{N2} \frac{P_{N2,in}}{\sqrt{T_{N2,in}}}$$

Total Mass Flowrate,

$$\dot{m}_{tot} = \dot{m}_{H2} + \dot{m}_{O2} + \dot{m}_{N2}$$

For the mass flowrate calculation, the discharge coefficient ( $C_d$ ), the area of the critical flow orifice or venturi ( $A_{ven}$ ) and two real gas corrections - the ideal sonic flow function ( $\Phi_i^*$ ) and the ratio of real to ideal sonic flow functions ( $\Phi^*/\Phi_i^*$ ) were required.  $\Phi_i^*$  and  $\Phi^*/\Phi_i^*$  are corrections for real gas effects and are derived in Reference 6.  $\Phi_i^*$  is strictly a function of the gas properties, while  $\Phi^*/\Phi_i^*$  is also a function of inlet temperature and pressure. These values

have been tabulated for hydrogen, oxygen, and nitrogen in Reference 6.

Characteristic Velocity,

$$c^* = \frac{P_{tot} A_t g_c}{\dot{m}_{tot}}$$

Thrust Coefficient,

$$C_f = \frac{F_{vac}}{P_{tot} A_t}$$

Specific Impulse,

$$I_{sp} = \frac{F_{vac}}{\dot{m}_{tot}}$$

Note that

$$I_{sp} = c^* C_f / g_c$$

Total chamber pressure,  $P_{tot}$ , was used in performance calculations. It was related to  $P_c$ , the static pressure measurement made in the injector, behind the combustion zone. The  $P_c$  measurement was corrected for pressure drop across the combustion zone (due to momentum loss) and then this quantity was converted into stagnation or total pressure using the estimated velocity of the gases in the combustion chamber. The pressure drop across the combustion zone was measured previously in another copper heat sink chamber of the same contour as the one tested in this study.

The rocket throat area,  $A_t$ , was corrected for thermal growth during firing, based on the throat temperature,  $T_{chamber}$ , (measured by a thermocouple) and coefficient of thermal expansion of the chamber material, i.e., copper. The constant  $g_c$  is the gravitational constant.

### Uncertainty Analysis

All measurements have an associated experimental error, where the error is defined as the difference between the measurement and the true value. These errors can be combined to provide the measurement uncertainty for a particular parameter, that is, the maximum error that might reasonably be expected. The uncertainty model for rocket testing recommended in Reference 7 was adopted for this study. The uncertainty analysis methodology is described in Appendix A. Any small bias errors were ignored as negligible in this analysis. For this study, then, no bias errors were assumed in the uncertainty analysis. The analysis is of random errors only.

The random uncertainty of the measured and calculated parameters was determined for every test firing conducted in this study. There was little variation in the uncertainty values, from test to test. Typical measurement uncertainty values are listed in Table 2.

The measurement uncertainties were generally around 1% or less for all of the parameters of interest. A low uncertainty in vacuum thrust was achieved in particular, due to the fact that careful attention was paid to the thrust measurement. There were generally six thrust calibrations and two thrust data acquisition error tests conducted for every test series, which increased the sample size (degrees of freedom) and reduced the measurement uncertainty.

### Results and Discussion

The experimental rocket performance parameters defined above, i.e., specific impulse ( $I_{sp}$ ), thrust coefficient ( $C_f$ ), and characteristic velocity ( $c^*$ ) were normalized to their theoretical one-dimensional equilibrium<sup>8</sup> values at the measured rocket chamber total pressure,  $P_{tot}$ , and inlet flow composition, including secondary nitrogen flow. The one-dimensional equilibrium<sup>8</sup> program is an industry standard computer program, which assumes that thermodynamic variations occur in only one direction, i.e., parallel to the rocket axis. Equilibrium, at each axial position, is that composition such that the free energy is minimized. This composition results in the theoretical maximum performance for the given rocket chamber total pressure and reference enthalpy of the inlet flow composition. The normalized performance parameters are defined as follows:

$$\eta_{I_{sp}} = \left[ \frac{I_{sp}}{I_{spODE}} \right]_{vac}$$

$$\eta_{C_f} = \left[ \frac{C_f}{C_{fODE}} \right]_{vac}$$

$$\eta_{c^*} = \frac{c^*}{c^*_{ODE}}$$

where the subscripts

*vac* – based on vacuum thrust

*ODE* – based on one-dimensional equilibrium

Values of  $\eta_{Isp}$ ,  $\eta_{C^*}$ , and  $\eta_{Cf}$  are given in Table 3 for relevant numerical cases computed in Reference 3. The value of  $\eta_{Isp}$  was given in the Reference 3. The value of  $\eta_{C^*}$  was assumed to be 1.0 in the Reference 3, but, by the definitions used in this paper, the secondary flow must be included and  $\eta_{C^*}$  was reduced to 0.926 for 8% secondary flow. This secondary flow had the effect of lowering the experimental characteristic velocity,  $c^*$ , of the rocket chamber, since it did not flow through the rocket throat and thereby, contribute to the chamber pressure,  $P_{tot}$ . The injection of secondary flow, therefore, was counted as a loss of  $c^*$  in this paper. The secondary flow interacted with the rocket flow as it flowed through the duct nozzle and influenced in the nozzle thrust coefficient. By definition, thrust coefficient efficiency,  $\eta_{Cf}$ , was calculated by the following equation:

$$\eta_{Cf} = \frac{\eta_{Isp}}{\eta_{c^*}}$$

The predicted specific impulse efficiency, thrust coefficient efficiency, and characteristic velocity efficiency, given in Table 3, are shown in Figure 7, 8, and 9, respectively, as a function of secondary flow for three different free expansions at  $L/D=5$ . Note the decrease in  $\eta_{Isp}$  and  $\eta_{Cf}$  as the free expansion percent increases and the increase in  $\eta_{Isp}$  and  $\eta_{Cf}$  as secondary flow increases. The  $\eta_{C^*}$  decreases with the addition of secondary flow as discussed above. Note that the increase in  $\eta_{Cf}$  and the decrease in  $\eta_{C^*}$  with the addition of secondary flow had canceling effects in  $\eta_{Isp}$ , but a slight increase was still predicted.

The experimental data for each test run for this paper is given in Appendix B.

Data for the baseline rocket and the five rocket-in-a-duct configurations was included. The theoretical one-dimensional equilibrium<sup>8</sup> performance was calculated at  $P_{tot}$  and at the experimentally measured mixture ratio, including gaseous nitrogen diluent.

The measured head end pressure,  $P_{head}$ , at the blind end of the duct for each test run was normalized to the rocket chamber total pressure and plotted in Figure 10 as a function of secondary flow for the five rocket-in-a-duct configurations tested. The curves are linear regression curve fits to aid in viewing the data. One notes that, for these tests, head end pressures are in the range of 0.2 to 1.3% of the rocket chamber pressure and that head end pressure rises with the addition of secondary flow. One also notes that larger free expansion area ratios result in lower head end pressures. There was also no discernable effect of duct length on head end pressure. These measurements indicated that head end pressure was controlled by the pressure in the free expansion zone and not by downstream pressure. A test at higher downstream pressure was conducted to verify that downstream pressure was not communicated to the pressure at the head end of the duct.

The measured specific impulse efficiency,  $\eta_{Isp}$ , thrust coefficient efficiency,  $\eta_{Cf}$ , and characteristic velocity efficiency,  $\eta_{C^*}$ , given in Tables B2, B3, and B6, for three different free expansions at  $L/D=5$  are shown in Figures 11, 12, and 13, respectively, as a function of secondary flow. The baseline rocket data given in Table B1 was plotted for reference. Note that there was

undesirable scatter in  $\eta_{C^*}$  shown in Figure 13. Ideally, this data would collapse to a single line as shown in Figure 9 for the numerical data. This scatter indicated that the performance of the injector could be sensitive to mixture ratio and chamber pressure, which influence the gaseous propellant mass-flows and their injection velocities. Also, the integrity of the seals could be different for each test setup, resulting in day-to-day variations in  $\eta_{C^*}$ . This could explain why the baseline rocket performance is higher than the other data in Figure 13.

Note that, as with the numerical results, there was a decrease in  $\eta_{Cf}$  as the free expansion percent increases and the increase in  $\eta_{Cf}$  as secondary flow increases shown in Figure 12. The  $\eta_{C^*}$  decreased with the addition of secondary flow as discussed previously and had the undesirable scatter discussed above. Note, again that the increase in  $\eta_{Cf}$  and the decrease in  $\eta_{C^*}$  with the addition of secondary flow had canceling effects in  $\eta_{Isp}$ , but there was a discernable peak in  $\eta_{Isp}$  at 4% secondary flow shown in Figure 11.

The measured specific impulse efficiency,  $\eta_{Isp}$ , thrust coefficient efficiency,  $\eta_{Cf}$ , and characteristic velocity efficiency,  $\eta_{C^*}$ , given in Tables B2, B4, and B5, for three different nozzle lengths are shown in Figures 14, 15, and 16, respectively, as a function of secondary flow. The baseline rocket data given in Table B1 was plotted for reference. Note again that there was undesirable scatter in  $\eta_{C^*}$  shown in Figure 16 and that  $\eta_{C^*}$  for the 3 diameter long duct had a low bias. Ideally, this data would collapse to a single line as

shown in Figure 9 for the numerical data. Again, the baseline rocket performance is higher than the other data in Figure 16.

Note that there was a decrease in  $\eta_{Cf}$  as the length of the duct increases and the increase in  $\eta_{Cf}$  as secondary flow increases as shown in Figure 15. The  $\eta_{C^*}$  decreased with the addition of secondary flow as discussed previously and had the undesirable scatter discussed above.

Note, again that the increase in  $\eta_{Cf}$  and the decrease in  $\eta_{C^*}$  with the addition of secondary flow had canceling effects in  $\eta_{Isp}$ , but there was a discernable peak in  $\eta_{Isp}$  at 4% secondary flow shown in Figure 14.

Finally, note that the computational data of Reference 3 predicted that larger nozzles have higher efficiencies than the small-scale ducts reported in this paper. In fact, performance of the rocket-in-a-duct with secondary flow was predicted to be comparable to that of other optimized rocket nozzles. Higher performance of larger nozzles can be anticipated due to the lower viscous losses, but this remains to be proven in a large-scale, rocket-in-a-duct.

## **Summary**

An understanding of the relevant physics of rocket-in-a-duct flows was experimentally tested in a 110 N class, gaseous hydrogen, gaseous oxygen, rocket altitude test facility. Copper heat sink type test apparatus was employed and industry standard rocket test procedures and uncertainty analyses were used. These tests simulated the relevant flow expansion physics and were economical to run. Facility thrust

random measurement error was within  $\pm 1\%$ . Five different rocket-in-a-duct configurations were tested with a secondary flow of gaseous nitrogen introduced at the blind end of the duct. The experimental specific impulse efficiency,  $\eta_{Isp}$ , thrust coefficient efficiency,  $\eta_{Cf}$ , and characteristic velocity efficiency,  $\eta_{C*}$  for three different free expansions at  $L/D=5$  and three different duct lengths with a free expansion between  $\epsilon=8$  to 23.5 were given as a function of secondary flow. There was undesirable scatter in  $\eta_{C*}$  which could be injector and/or seal related. There was a decrease in  $\eta_{Cf}$  as the free expansion percent increased and

as the length of the duct increased. An increase in  $\eta_{Cf}$  occurred as secondary flow increased. The  $\eta_{C*}$  decreased with the addition of secondary flow by definition. The increase in  $\eta_{Cf}$  and the decrease in  $\eta_{C*}$  with the addition of secondary flow had canceling effects in  $\eta_{Isp}$ , but there was a discernable peak in  $\eta_{Isp}$  at 4% secondary flow. Prior numerical modeling of larger rocket-in-a-duct engines predicted possible nozzle performance comparable to that of other optimized rocket nozzles, but this remains to be proven in a large-scale, rocket-in-a-duct.

### **References**

1. Daines, R. and Segal, C., "Combined Rocket and Airbreathing Systems for Space Launch Applications", Journal of Propulsion and Power, Vol. 14, No. 5, pp 605-612, September-October 1998
2. Trefny, C., "An Air-Breathing Launch Vehicle Concept for Single-Stage-to-Orbit", AIAA 99-2730, 35<sup>th</sup> AIAA/ASME/SAE/ASEE Joint Propulsion Conference, Los Angeles, June 1999
3. Steffen, C. J., Smith, T. D., Yungster, S., and Keller, D. J., "Rocket Based Combined-Cycle Analysis Using NPARC", AIAA 98-0954, 36<sup>th</sup> Aerospace Sciences Meeting, Reno, January 1998
4. Robinson, P. J., "Space Station Auxiliary Thrust Chamber Technology", NASA CR-185296, July 1990
5. Arrington, L. A. and Schneider, S. J., "Low Thrust Rocket Test Facility", AIAA 90-2503, 26<sup>th</sup> AIAA/ASME/SAE/ASEE Joint Propulsion Conference, Orlando, July 1990
6. "Fluid Meters: Their Theory and Application", American Society of Mechanical Engineers, 1971
7. "Handbook for Estimating the Uncertainty in Measurements Made with Liquid Propellant Rocket Engine Systems", CPIA 180, Chemical Propulsion Information Agency, April 1969
8. McBride, B. and Gordon, S., "Computer Program for Calculation of Complex Chemical Equilibrium Compositions and Applications", NASA RP-1311, June 1996

Combustion Chamber		Throat	Nozzle	Duct				
length~cm	diameter~cm	diameter~cm	$\epsilon$	L~cm	D~cm	$\epsilon$	% $\epsilon$ free	L/D
5.08	2.54	1.278	8	24.88	4.976	15.2	47.4	5
5.08	2.54	1.278	8	18.55	6.185	23.5	66	3
5.08	2.54	1.278	8	30.92	6.185	23.5	66	5
5.08	2.54	1.278	8	43.29	6.185	23.5	66	7
5.08	2.54	1.278	8	36.92	7.384	33.4	76	5

Table 1. Rocket-in-a-duct configurations tested.

Parameter	Measurement Uncertainty (%)
Total Chamber Pressure	0.57
Vacuum Force	0.47
Oxygen Mass Flowrate	1.07
Hydrogen Mass Flowrate	1.01
Nitrogen Mass Flowrate	1.00
Total Mass Flowrate	0.44
Mixture Ratio	1.43
Characteristic Velocity	1.04
Thrust Coefficient	0.73
Specific Impulse	0.95

Table 2. Typical Measurement Uncertainty Values

Case	$P_c \sim \text{Mpa}$	Sec. Flow %	Free Exp $\epsilon$	% $\epsilon$ Free	$\eta$ Isp	$\eta$ C*	$\eta$ Cf
4	2.1	0	4-200	0.98	0.778	1.000	0.778
12	8.3	0	4-200	0.98	0.797	1.000	0.797
15	8.3	8	20-200	0.90	0.880	0.926	0.951
19	2.1	0	20-200	0.90	0.867	1.000	0.867
20	2.1	8	4-200	0.98	0.800	0.926	0.864
35	8.3	8	20-39	0.49	0.901	0.926	0.973

Table 3. Computational results for rocket-in-a-duct, L/D=5, constant area. (Reference 3)

## **Appendix A: Uncertainty Analysis Methodology**

Every measurement and every parameter calculated from measurements have an associated uncertainty value. Reference 7 has a recommended methodology for determining the measurement uncertainty in rocket testing. This methodology was adopted for the testing conducted in this study and is described below.

The measured parameters in this study for which there is an associated error are summarized in Table A1. The sources of error for each parameter can be divided into three categories: calibration errors, data acquisition errors, and data reduction errors. Each of these elemental sources of errors can have two components, a precision (random) error and a bias (fixed) error associated with it.

The bias error is a constant, systematic deviation from the true value. The calibration of the measuring instruments was used to eliminate large known biases. Control of the measuring process was used to insure that there were no large unknown bias errors (such as thermal drift). Any small bias errors were ignored as negligible in this analysis. For this study, then, no bias errors were assumed in the uncertainty analysis. The analysis is of random errors only.

The precision error is the variation seen in repeated measurements and is characterized by the precision error index, ( $s$ ). The precision index for a set of repeated measurements is defined by:

$$s = \sqrt{\frac{\sum_{i=1}^N (x_i - \bar{x})^2}{N - 1}}$$

where  $N$  = number of measurements made,  $x_i$  = the individual measurements, and  $\bar{x}$  = the average value of the individual measurements.

The sample size or the number of degrees of freedom ( $df$ ) associated with the above precision index is defined as

$$df = N - 1$$

The calibration precision errors in the measuring instruments were determined through offline calibration (sonic venturis), in-situ calibration (load cell), or manufacturers' specifications (pressure transducers, thermocouples). For geometric parameters (throat and nozzle areas), the precision error was estimated as the square of the specified diameter tolerance. For the sonic flow function ratios, which were estimated from curve fits of table data, precision error was determined from the Standard Estimate of Error ( $S_{EE}$ ),

$$S_{EE} = \sqrt{\frac{\sum_{i=1}^N (y_i - y_{i,c})^2}{N - C}}$$

where  $y_i$  = the data point,  $y_{i,c}$  = the equivalent calculated value from the curve fit,  $N$  = number of data points, and  $C$  = number constants used in the curve fit.

Here the number of degrees of freedom was defined as

$$df = N - C.$$

Data acquisition errors are those associated with the output signal from the measuring instrument to the recording device. Sources of errors here include the excitation voltage, signal conditioning, and signal gain. In this study, data acquisition errors were determined by end-to-end calibrations (load cell) or from the manufacturer's calibration data on the data acquisition cards (pressure transducers and thermocouples). The data reduction errors are those due to computer resolution and, for this study, were assumed to be zero.

The elemental sources of error for the measured parameters were combined using the root sum square. So the calibration precision errors ( $S_{cal}$ ) and data acquisition precision errors ( $S_{da}$ ) were be combined such that for a measuring instrument,  $M_i$ ,

$$S_{Mi} = \sqrt{S_{cal}^2 + S_{da}^2}$$

The number of degrees of freedom was defined as,

$$df_{Mi} = \frac{[S_{cal}^2 + S_{da}^2]^2}{\frac{S_{cal}^4}{df_{cal}} + \frac{S_{da}^4}{df_{da}}}$$

Performance parameters, such as specific impulse, thrust coefficient, and characteristic velocity were calculated from the measured parameters. Parameters such as vacuum force and mass flowrate are determined from measured parameters. The calculated parameters used in this study are summarized in Table A2.

It was necessary to propagate the errors in the measured parameters to calculated parameters. The error propagation was approximated with Taylor's series methods. Assume that the performance parameter,  $P_j$ , is calculated from  $N$  measured parameters such that,

$$P_j = f(M_1, \dots, M_i, \dots, M_N)$$

Then the precision error for  $P_j$  was calculated from the precision errors of the measured parameters from

$$S_{Pj} = \sqrt{\sum_{i=1}^N \left[ \left( \frac{\partial P_j}{\partial M_i} \right) (S_{Mi}) \right]^2}$$

The number of degrees of freedom for  $P_j$  can determined from

$$df_{Pj} = \frac{\left[ \sum_{i=1}^N \left[ \left( \frac{\partial P_j}{\partial M_i} \right) (S_{Mi}) \right]^2 \right]^2}{\sum_{i=1}^N \left[ \frac{\left[ \left( \frac{\partial P_j}{\partial M_i} \right) (S_{Mi}) \right]^4}{df_{Mi}} \right]}$$

The partial derivative,  $\delta P_j / \delta M_i$ , is called the influence coefficient and is the first term in a Taylor's series expansion. So, the partial derivative of the performance parameter with respect to each measurement in the performance equation must be found for error propagation. Propagation must be done with every parameter for which an error might exist. That is, the error of every calculated parameter in Table A2 must be related back to the error of every appropriate measured parameter in Table A1. For example, the influence of the precision error in the hydrogen inlet pressure measurement (used for hydrogen mass flowrate) on the specific



impulse error would be determined by the derivative of the specific impulse equation with respect to the hydrogen inlet pressure (imbedded in the total mass flowrate parameter).

The value for measurement uncertainty for the performance parameter  $P_j$ , used to express a reasonable limit for error was defined in Reference 7 as,

$$U_{P_j} = \pm (B_{P_j} + t_{95,df_{P_j}} S_{P_j})$$

where  $S_{P_j}$  = precision error,  $B_{P_j}$  = bias error, and  $t_{95}$  = Students number, the 95th percentile point for the two-tailed Students “t” distribution. The measurement uncertainty,  $U_{P_j}$ , was a statistical band within which the true value of the measured parameter was expected to lie, at a 95% confidence

level. In this analysis, the bias error is zero.

The Students number was used to inflate the value of  $U_{P_j}$  to reduce the risk of underestimating  $S_{P_j}$  when a small sample was used to calculate  $S_{P_j}$ . The  $t_{95,df_{P_j}}$  value was a function of the size of the sample (the number of degrees of freedom,  $df_{P_j}$ ) used in calculating  $S_{P_j}$ . For small sample sizes  $t_{95,df_{P_j}}$  will be large, while for larger samples  $t_{95,df_{P_j}}$  will be smaller. The value of  $t_{95,\infty} = 1.96$  for an infinite number of degrees of freedom and  $t_{95,30} = 2.04$  at 30 degrees of freedom, so a value of 2.0 was assumed for  $t_{95}$  is used for  $df = 30$  or above.

Measured Parameters
Chamber Pressure
Ambient Pressure
Site Force
Rocket Throat Area
Rocket Nozzle Exit Area
Hydrogen Venturi Discharge Coefficient
Hydrogen Venturi Sonic Flow Function Ratio
Hydrogen Venturi Throat Area
Hydrogen Venturi Inlet Pressure
Hydrogen Venturi Inlet Temperature
Oxygen Venturi Discharge Coefficient
Oxygen Venturi Sonic Flow Function Ratio
Oxygen Venturi Throat Area
Oxygen Venturi Inlet Pressure
Oxygen Venturi Inlet Temperature
Nitrogen Venturi Discharge Coefficient
Nitrogen Venturi Sonic Flow Function Ratio
Nitrogen Venturi Throat Area
Nitrogen Venturi Inlet Pressure
Nitrogen Venturi Inlet Temperature

Table A1: Measured Parameters

<b>Calculated Parameters</b>
Total Chamber Pressure
Hydrogen Mass Flowrate
Oxygen Mass Flowrate
Nitrogen Mass Flowrate
Total Mass Flowrate
Mixture Ratio
Vacuum Force
Characteristic Velocity
Thrust Coefficient
Specific Impulse

Table A2: Calculated Parameters

## Appendix B. Experimental Data

Ptot(kPa)	MR	%N2	Isp(sec)	c*(m/sec)	Cf	Fvac(N)	mtot(g/s)	Isp-eff	c*-eff	Cf-eff	Phead(kPa)	Pamb(kPa)
462.3	3.66	N/A	342	2297	1.462	86.6	25.8	0.784	0.914	0.858	N/A	1.69
462.3	3.96	N/A	341	2287	1.464	87.4	26.1	0.785	0.919	0.855	N/A	1.58
469.2	3.87	N/A	342	2301	1.456	88.2	26.3	0.786	0.922	0.852	N/A	1.61
483.0	3.89	N/A	339	2283	1.457	90.8	27.3	0.779	0.915	0.852	N/A	1.61
496.8	3.82	N/A	346	2335	1.454	93.0	27.4	0.795	0.934	0.851	N/A	1.68
517.5	3.81	N/A	348	2350	1.452	96.0	28.1	0.799	0.939	0.851	N/A	1.75
552.0	4.01	N/A	339	2295	1.450	102.3	30.7	0.781	0.923	0.846	N/A	1.68
558.9	3.97	N/A	346	2345	1.449	104.2	30.7	0.796	0.942	0.846	N/A	1.77
565.8	3.94	N/A	345	2331	1.450	105.4	31.2	0.793	0.935	0.847	N/A	1.84
655.5	3.91	N/A	342	2332	1.437	121.0	36.1	0.786	0.934	0.841	N/A	1.80
662.4	4.03	N/A	341	2314	1.443	122.8	36.7	0.785	0.930	0.842	N/A	1.68

Table B1. Test data – Baseline Rocket

Ptot(kPa)	MR	%N2	Isp(sec)	c*(m/sec)	Cf	Fvac(N)	mtot(g/s)	Isp-eff	c*-eff	Cf-eff	Phead(kPa)	Pamb(kPa)
462.3	3.99	0.0	331	2274	1.427	84.5	26.0	0.715	0.915	0.781	1.70	1.79
462.3	3.97	0.0	328	2269	1.419	84.3	26.2	0.708	0.912	0.777	1.70	1.71
462.3	3.97	2.4	335	2210	1.488	88.4	26.9	0.731	0.898	0.816	2.88	1.61
462.3	4.01	2.5	335	2207	1.486	88.1	26.8	0.732	0.898	0.814	2.75	1.66
469.2	3.99	2.4	334	2198	1.490	89.6	27.4	0.729	0.893	0.816	3.15	1.70
469.2	4.02	4.3	333	2152	1.517	91.5	28.0	0.734	0.883	0.831	3.55	1.68
476.1	3.99	0.0	329	2284	1.412	86.2	26.7	0.710	0.919	0.773	1.70	1.79
476.1	4.07	0.8	331	2228	1.456	88.8	27.4	0.718	0.902	0.796	2.36	1.75
476.1	4.11	1.9	331	2186	1.483	90.4	27.9	0.722	0.890	0.809	2.88	1.75
476.1	4.03	9.7	320	2062	1.520	92.8	29.6	0.724	0.866	0.835	3.95	1.57
558.9	4.04	0.0	329	2262	1.427	101.8	31.5	0.711	0.910	0.781	1.96	1.73
558.9	4.10	0.0	332	2260	1.442	103.4	31.7	0.717	0.912	0.788	2.49	1.77
558.9	4.12	0.9	333	2243	1.458	105.0	32.1	0.723	0.909	0.796	3.15	1.70
558.9	4.15	1.9	332	2201	1.480	106.6	32.7	0.724	0.897	0.808	3.68	1.70
565.8	4.06	2.5	337	2224	1.484	107.2	32.4	0.736	0.905	0.812	3.95	1.70
565.8	4.13	4.5	330	2152	1.503	108.6	33.6	0.728	0.886	0.822	4.34	1.62
565.8	4.11	9.9	318	2056	1.518	109.8	35.2	0.720	0.866	0.832	4.87	1.61
669.3	4.00	0.0	335	2286	1.438	123.9	37.6	0.723	0.918	0.788	3.42	1.72
669.3	3.98	0.9	335	2258	1.455	124.5	37.8	0.726	0.910	0.798	3.82	1.68
669.3	3.99	2.0	334	2222	1.473	126.2	38.5	0.728	0.900	0.808	4.47	1.63
669.3	4.07	2.6	332	2227	1.461	125.3	38.5	0.726	0.906	0.800	4.60	1.61
669.3	4.06	4.7	331	2188	1.485	127.5	39.2	0.731	0.899	0.814	5.26	1.55
669.3	3.98	10.1	317	2085	1.490	127.4	41.0	0.718	0.875	0.820	5.80	1.62
676.2	4.10	0.0	330	2292	1.413	122.9	37.9	0.713	0.923	0.773	2.36	1.83

Table B2. Test data, Rocket-in-a-Duct, 6.18 cm dia., 5 dia. Long

Ptot(kPa)	MR	%N2	Isp(sec)	c*(m/sec)	Cf	Fvac(N)	mtot(g/s)	Isp-eff	c*-eff	Cf-eff	Phead(kPa)	Pamb(kPa)
462.3	3.91	0.0	328	2269	1.419	84.8	26.3	0.724	0.910	0.796	2.75	1.58
462.3	4.09	0.0	318	2190	1.425	84.2	26.9	0.703	0.884	0.796	2.62	1.44
462.3	3.91	4.3	327	2177	1.473	88.0	27.4	0.736	0.890	0.827	5.93	1.45
462.3	3.91	10.0	312	2065	1.481	88.4	28.9	0.722	0.866	0.833	6.06	1.61
469.2	4.09	0.0	323	2241	1.413	84.8	26.8	0.714	0.905	0.789	2.75	1.56
469.2	3.90	2.4	329	2210	1.462	87.4	27.0	0.734	0.896	0.821	5.40	1.49
476.1	4.05	0.0	325	2233	1.425	87.6	27.5	0.718	0.900	0.797	2.75	1.49
476.1	4.14	0.4	328	2230	1.442	88.0	27.4	0.727	0.903	0.804	3.68	1.52
476.1	4.20	0.9	324	2216	1.434	87.7	27.6	0.720	0.902	0.799	4.21	1.56
476.1	4.17	1.9	327	2195	1.460	89.1	27.8	0.730	0.896	0.814	5.00	1.52
558.9	4.15	0.4	326	2236	1.430	102.8	32.2	0.722	0.905	0.798	4.47	1.63
565.8	4.20	0.0	322	2239	1.411	102.3	32.3	0.756	0.906	0.787	3.42	1.68
565.8	4.20	0.9	324	2202	1.443	104.5	32.8	0.720	0.895	0.804	5.13	1.60
572.7	4.15	0.0	324	2258	1.409	103.2	32.4	0.716	0.912	0.786	3.42	1.66
572.7	4.20	1.9	323	2189	1.447	106.0	33.4	0.721	0.893	0.807	6.19	1.56
572.7	4.16	9.8	308	2066	1.464	107.4	35.5	0.713	0.871	0.820	7.51	1.97
579.6	4.09	2.3	330	2235	1.447	107.2	33.1	0.737	0.910	0.809	6.59	1.45
579.6	4.16	4.3	322	2164	1.459	108.9	34.5	0.726	0.891	0.816	7.38	1.60
662.4	4.09	0.0	323	2269	1.395	119.1	37.6	0.713	0.914	0.780	4.08	1.84
662.4	4.07	0.4	328	2259	1.423	121.1	37.6	0.726	0.911	0.796	5.40	1.92
662.4	4.10	0.9	328	2250	1.429	121.9	37.9	0.728	0.910	0.799	6.19	1.66
662.4	4.12	1.9	327	2218	1.446	123.2	38.4	0.729	0.901	0.809	7.25	1.66
669.3	4.15	2.5	326	2200	1.452	124.1	38.8	0.729	0.897	0.812	7.91	1.65
676.2	3.99	4.6	323	2189	1.448	126.1	39.7	0.728	0.896	0.813	8.57	1.80
683.1	4.01	0.0	328	2283	1.408	122.8	38.2	0.724	0.917	0.789	4.21	1.82
683.1	3.96	9.8	311	2083	1.463	127.5	41.8	0.719	0.872	0.824	8.57	2.27

Table B3. Test Data, Rocket-in-a-Duct, 4.98 cm dia., 5 dia. Long

Ptot(kPa)	MR	%N2	Isp(sec)	c*(m/sec)	Cf	Fvac(N)	mtot(g/s)	Isp-eff	c*-eff	Cf-eff	Phead(kPa)	Pamb(kPa)
462.3	4.01	0.0	320	2167	1.449	86.4	27.5	0.691	0.873	0.793	1.57	1.70
462.3	4.06	0.0	317	2166	1.436	85.7	27.5	0.685	0.874	0.785	1.70	1.73
462.3	4.02	2.5	327	2130	1.508	90.1	28.0	0.715	0.867	0.825	3.15	1.61
462.3	4.10	9.6	311	1962	1.554	92.8	30.4	0.704	0.826	0.852	3.68	1.70
469.2	3.97	0.9	325	2174	1.466	87.7	27.5	0.705	0.877	0.803	2.23	1.64
469.2	4.00	1.9	327	2154	1.489	89.0	27.7	0.712	0.874	0.815	2.75	1.60
469.2	4.06	4.3	323	2085	1.520	91.1	28.7	0.712	0.856	0.832	3.55	1.61
476.1	4.03	0.0	323	2207	1.436	87.6	27.6	0.698	0.889	0.785	1.70	1.75
476.1	4.25	0.0	317	2142	1.452	88.3	28.4	0.686	0.870	0.789	1.70	1.73
476.1	4.09	0.3	322	2172	1.453	88.6	28.0	0.697	0.878	0.793	2.09	1.67
558.9	4.08	0.0	327	2224	1.442	103.6	32.3	0.706	0.896	0.788	1.96	2.04
558.9	4.09	0.0	325	2198	1.448	103.5	32.5	0.702	0.886	0.791	1.96	2.02
558.9	4.15	2.4	329	2144	1.505	108.1	33.5	0.719	0.875	0.822	3.95	1.89
558.9	4.12	10.0	311	1996	1.529	109.3	35.8	0.705	0.841	0.838	4.47	2.03
565.8	4.12	0.4	327	2206	1.452	105.4	32.9	0.708	0.892	0.793	2.49	2.00
565.8	4.23	0.9	325	2180	1.461	106.0	33.2	0.706	0.887	0.795	2.75	1.95
565.8	4.24	1.9	327	2157	1.487	108.0	33.7	0.714	0.881	0.810	3.42	1.93
565.8	4.36	4.4	322	2093	1.511	110.1	34.8	0.712	0.868	0.821	4.21	1.90
565.8	4.30	4.4	325	2095	1.519	110.3	34.6	0.718	0.867	0.827	4.34	1.90
669.3	4.11	0.0	327	2245	1.427	122.6	38.2	0.706	0.905	0.780	2.36	2.35
669.3	4.05	0.0	327	2237	1.433	122.7	38.2	0.706	0.900	0.784	2.36	2.33
669.3	4.17	0.4	327	2211	1.452	124.8	38.8	0.708	0.895	0.792	3.02	2.33
669.3	4.11	0.9	331	2224	1.461	125.5	38.6	0.718	0.900	0.799	3.42	2.25
669.3	4.10	1.9	332	2193	1.486	127.6	39.1	0.723	0.891	0.813	4.21	2.24
669.3	4.13	2.5	329	2156	1.494	128.4	39.8	0.719	0.879	0.817	4.60	2.21
669.3	4.10	4.7	327	2125	1.510	129.8	40.4	0.722	0.873	0.827	5.13	2.21
669.3	4.18	9.8	314	2024	1.521	130.5	42.4	0.711	0.853	0.833	5.40	2.45

Table B4. Test Data, Rocket-in-a-Duct, 6.18 cm dia., 3 dia. Long

Ptot(kPa)	MR	%N2	Isp(sec)	c*(m/sec)	Cf	Fvac(N)	mtot(g/s)	Isp-eff	c*-eff	Cf-eff	Phead(kPa)	Pamb(kPa)
476.1	3.93	0.0	331	2306	1.408	86.5	26.6	0.714	0.925	0.772	1.70	1.91
476.1	4.21	0.0	317	2191	1.420	86.9	27.9	0.686	0.888	0.773	1.70	1.75
476.1	4.03	0.0	323	2252	1.409	86.3	27.2	0.698	0.907	0.770	1.70	1.86
476.1	4.23	0.0	315	2178	1.417	86.5	28.0	0.682	0.884	0.771	1.70	1.73
476.1	3.98	2.4	333	2217	1.474	90.7	27.7	0.727	0.901	0.808	3.28	1.65
476.1	3.98	4.3	328	2161	1.487	90.9	28.3	0.723	0.885	0.816	3.55	1.56
483.0	4.09	0.3	325	2234	1.427	88.0	27.6	0.703	0.903	0.779	2.09	1.70
483.0	4.10	0.8	326	2216	1.441	89.4	28.0	0.707	0.898	0.787	2.36	1.75
483.0	4.10	1.9	326	2188	1.462	90.4	28.3	0.711	0.891	0.798	2.88	1.64
483.0	4.00	9.8	311	2062	1.480	91.1	29.8	0.704	0.866	0.813	3.82	1.58
565.8	4.24	0.0	322	2247	1.405	102.0	32.3	0.697	0.911	0.765	2.09	1.83
572.7	4.24	0.4	326	2240	1.427	104.5	32.7	0.707	0.909	0.777	2.49	1.70
572.7	4.25	0.9	324	2221	1.432	105.5	33.2	0.704	0.904	0.779	3.02	1.66
572.7	4.34	1.9	322	2180	1.450	106.9	33.8	0.703	0.894	0.788	3.55	1.61
579.6	4.17	0.0	324	2266	1.401	103.6	32.6	0.700	0.916	0.764	2.09	1.75
579.6	4.06	2.5	329	2221	1.454	108.0	33.4	0.719	0.904	0.796	3.95	1.50
579.6	4.29	4.4	321	2139	1.472	108.9	34.6	0.709	0.885	0.802	4.34	1.58
579.6	4.31	9.7	305	2032	1.471	108.9	36.4	0.691	0.861	0.803	4.60	1.66
669.3	3.98	0.0	325	2283	1.396	119.5	37.5	0.701	0.916	0.766	2.49	1.54
669.3	4.11	0.8	323	2231	1.420	122.3	38.6	0.700	0.902	0.776	3.42	1.52
669.3	4.13	1.9	324	2201	1.443	124.3	39.1	0.706	0.895	0.789	4.21	1.55
676.2	4.05	0.0	324	2272	1.397	121.6	38.3	0.699	0.914	0.765	2.49	1.45
676.2	4.05	0.4	324	2260	1.404	121.4	38.2	0.701	0.911	0.768	3.02	1.50
676.2	4.14	0.9	321	2224	1.417	122.4	38.8	0.696	0.901	0.774	3.42	1.48
676.2	4.05	2.6	328	2224	1.447	124.9	38.8	0.717	0.904	0.793	4.60	1.45
676.2	4.12	4.6	321	2167	1.454	126.5	40.1	0.708	0.891	0.796	5.00	1.59
676.2	4.12	9.8	307	2062	1.461	126.7	42.0	0.695	0.868	0.801	5.53	1.69

Table B5. Test data, Rocket-in-a-duct, 6.18 cm dia., 7 dia. long

Ptot(kPa)	MR	%N2	Isp(sec)	c*(m/sec)	Cf	Fvac(N)	mtot(g/s)	Isp-eff	c*-eff	Cf-eff	Phead(kPa)	Pamb(kPa)
476.1	4.16	0.0	319	2177	1.436	87.1	27.9	0.679	0.881	0.770	1.17	1.64
476.1	4.35	0.0	315	2186	1.415	86.3	27.9	0.672	0.891	0.755	1.30	1.79
483.0	3.88	0.0	330	2281	1.417	88.1	27.2	0.702	0.914	0.767	1.30	1.86
483.0	4.22	0.0	316	2176	1.425	88.1	28.4	0.673	0.882	0.763	1.17	1.64
483.0	4.09	0.4	328	2227	1.444	89.0	27.6	0.699	0.901	0.776	1.44	1.81
483.0	4.04	0.9	330	2234	1.448	89.6	27.7	0.705	0.904	0.780	1.57	1.75
483.0	4.04	1.9	332	2221	1.465	91.0	27.9	0.712	0.902	0.789	1.83	1.70
489.9	4.04	2.3	327	2169	1.478	92.3	28.8	0.703	0.883	0.796	2.09	1.61
489.9	4.06	4.2	323	2114	1.500	94.2	29.7	0.701	0.868	0.809	2.23	1.55
489.9	4.08	9.5	314	2024	1.522	95.8	31.1	0.699	0.851	0.822	2.62	1.54
489.9	4.10	14.0	304	1941	1.534	96.7	32.5	0.693	0.834	0.830	2.75	1.60
572.7	4.09	0.0	328	2265	1.422	105.0	32.6	0.698	0.913	0.765	1.44	1.84
579.6	4.26	0.0	318	2212	1.412	105.2	33.7	0.677	0.897	0.756	1.44	1.75
579.6	4.13	0.4	329	2246	1.437	106.4	32.9	0.701	0.909	0.772	1.70	1.79
579.6	4.14	0.9	329	2237	1.444	107.2	33.2	0.703	0.907	0.776	1.96	1.75
579.6	4.20	1.9	328	2190	1.468	108.9	33.8	0.704	0.894	0.788	2.23	1.70
586.5	4.32	2.3	324	2164	1.469	110.6	34.7	0.698	0.888	0.786	2.49	1.61
586.5	4.32	4.3	323	2122	1.491	112.3	35.4	0.702	0.878	0.799	3.02	1.61
586.5	4.31	9.4	314	2028	1.516	114.4	37.2	0.700	0.858	0.814	3.28	1.66
669.3	4.04	0.9	331	2259	1.439	123.8	38.1	0.707	0.912	0.776	2.23	1.72
676.2	4.08	0.0	327	2264	1.417	123.5	38.5	0.695	0.912	0.763	1.70	1.74
676.2	4.11	1.9	329	2230	1.447	125.3	38.8	0.706	0.906	0.779	2.62	1.62
676.2	4.09	2.5	329	2200	1.467	127.7	39.6	0.708	0.896	0.791	3.02	1.63
683.1	4.02	0.0	332	2296	1.416	123.7	38.0	0.706	0.922	0.764	1.70	1.81
683.1	4.11	0.4	331	2266	1.433	125.5	38.6	0.705	0.915	0.771	2.09	1.81
683.1	4.12	4.6	325	2155	1.477	129.3	40.6	0.706	0.886	0.796	3.42	1.65
683.1	4.15	9.6	313	2048	1.497	131.2	42.7	0.697	0.862	0.808	3.82	1.70

Table B6. Test data, Rocket-in-a-duct, 7.38 cm dia., 5 dia. long





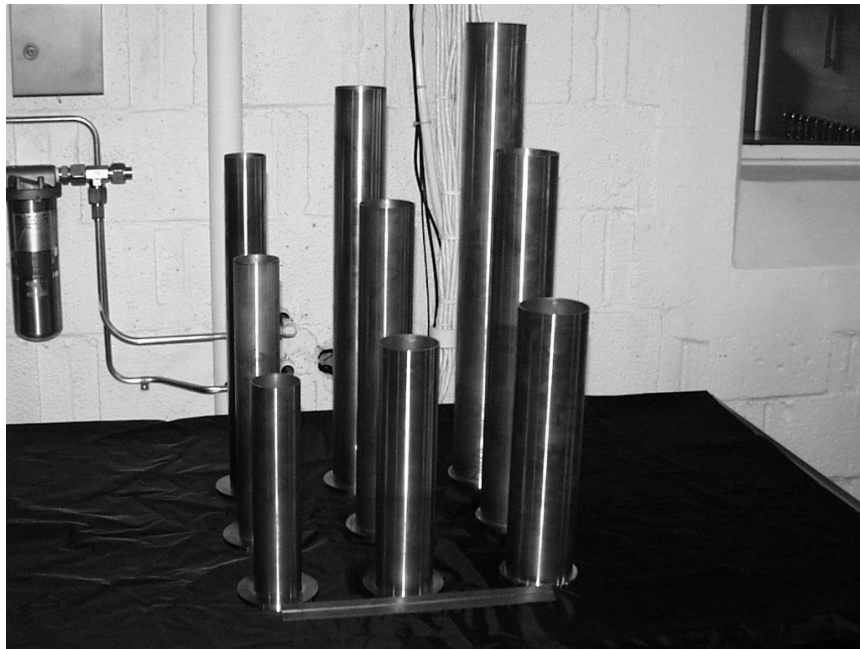
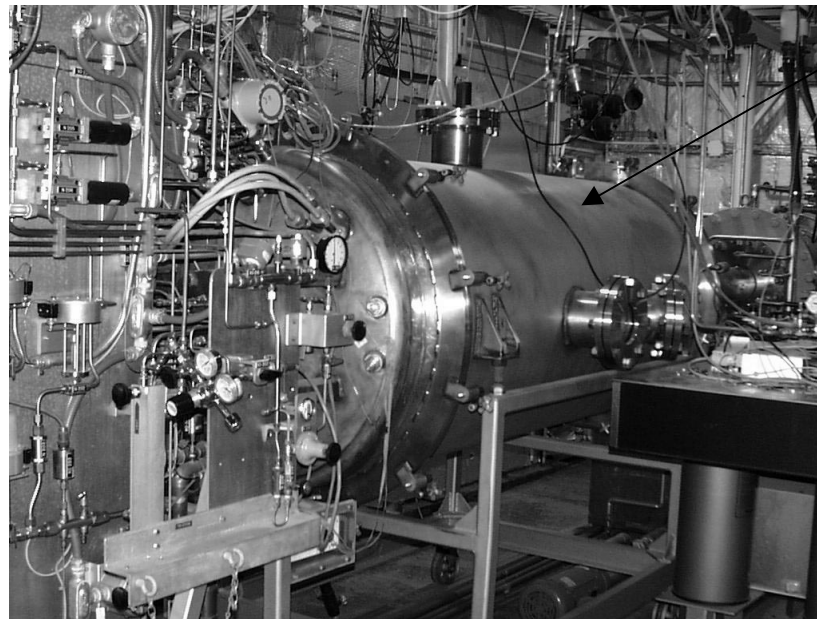


Figure 3. Various copper ducts fabricated for the test series from commercial pipe

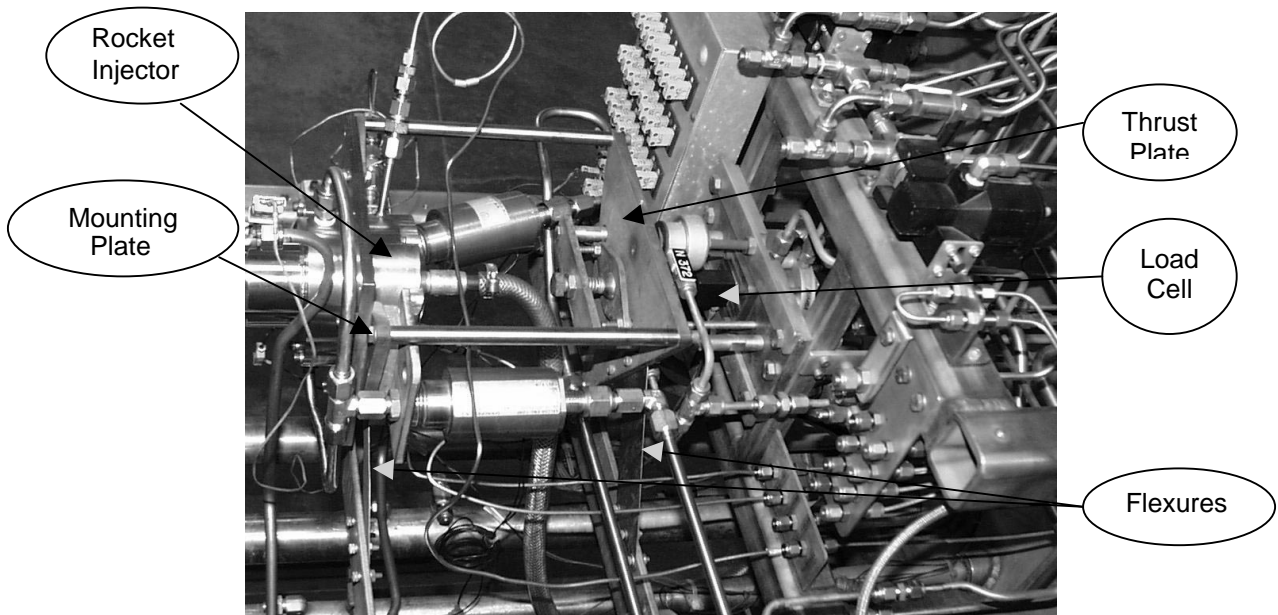


Figure 4. Rocket-in-a-duct test configuration



Altitude  
Chamber

Figure 5. Research Combustion Laboratory Cell-11



Rocket  
Injector

Mounting  
Plate

Thrust  
Plate

Load  
Cell

Flexures

Figure 6. Horizontally-oriented thrust stand

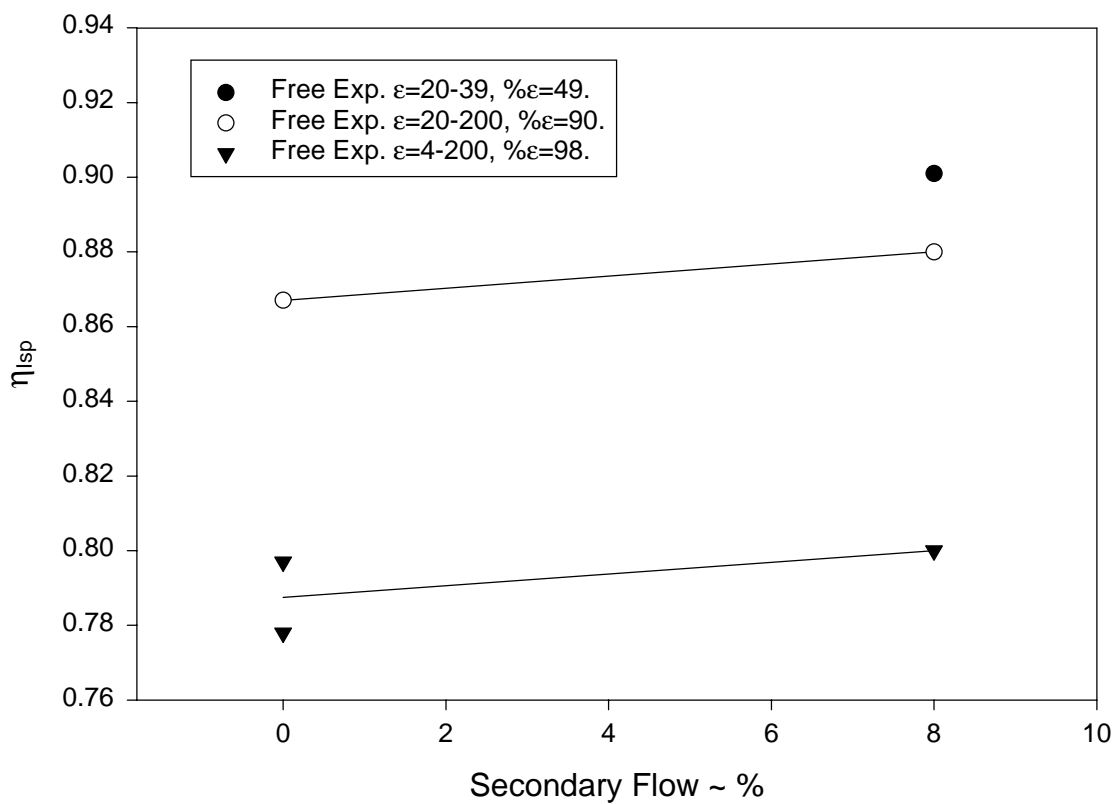


Figure 7. Predicted specific impulse efficiency of a rocket-in-a-duct as a function of secondary flow and free expansion area ratio for  $L/D=5$ , constant area duct. (CFD data from Reference 3.)

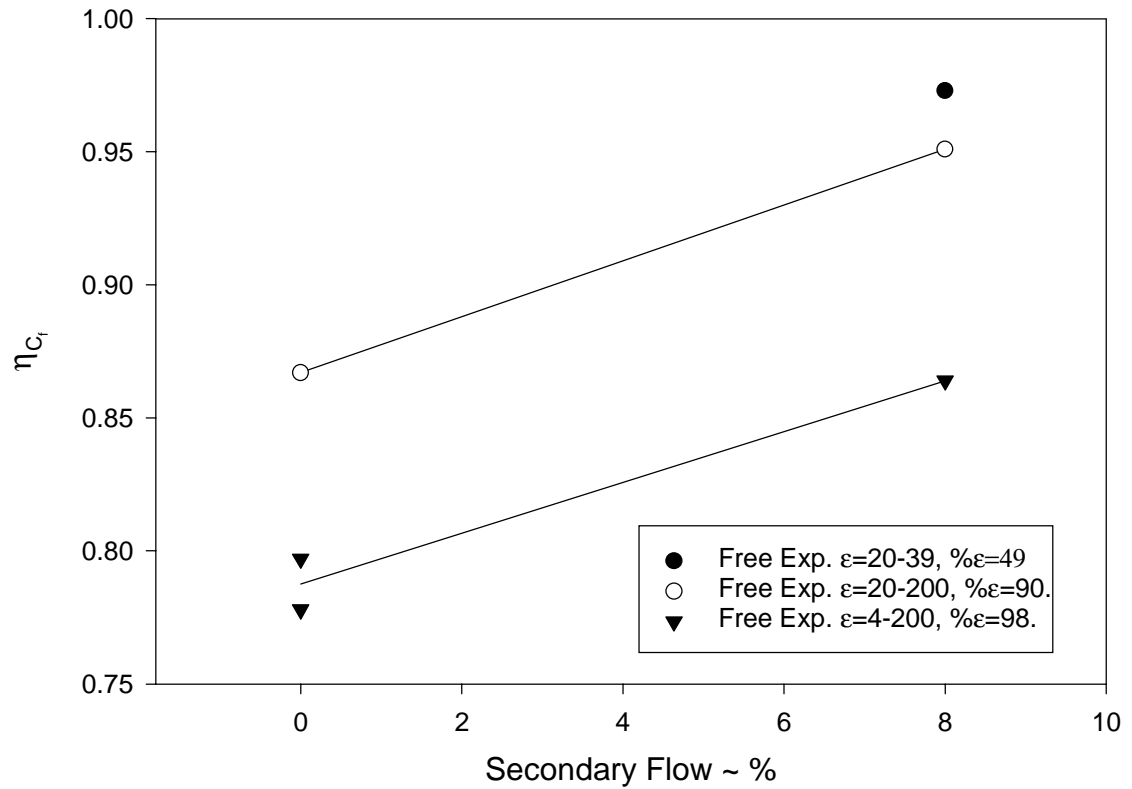


Figure 8. Predicted thrust coefficient efficiency of a rocket-in-a-duct nozzle as a function of secondary flow and free expansion area ratio for  $L/D=5$ , constant area duct. (CFD data from Reference 3.)

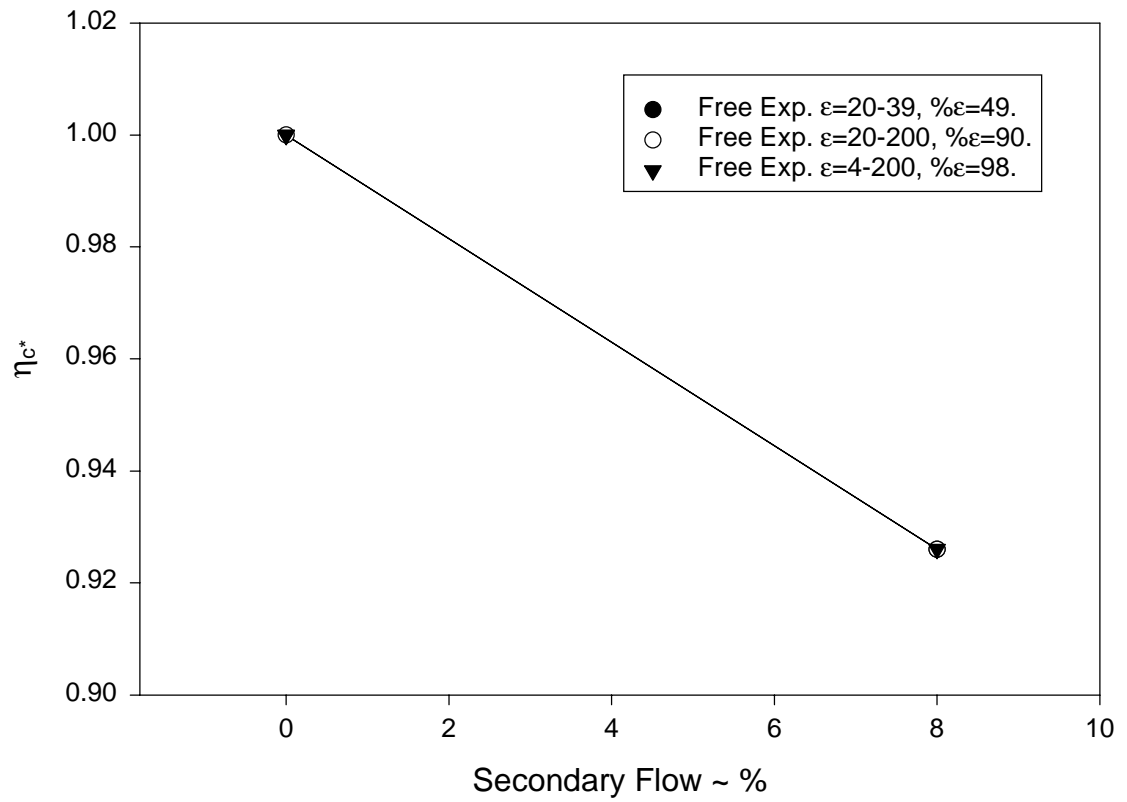


Figure 9. Characteristic velocity efficiency of a rocket-in-a-duct as a function of secondary flow and free expansion area ratio for  $L/D=5$ , constant area duct. (CFD data from Reference 3.)

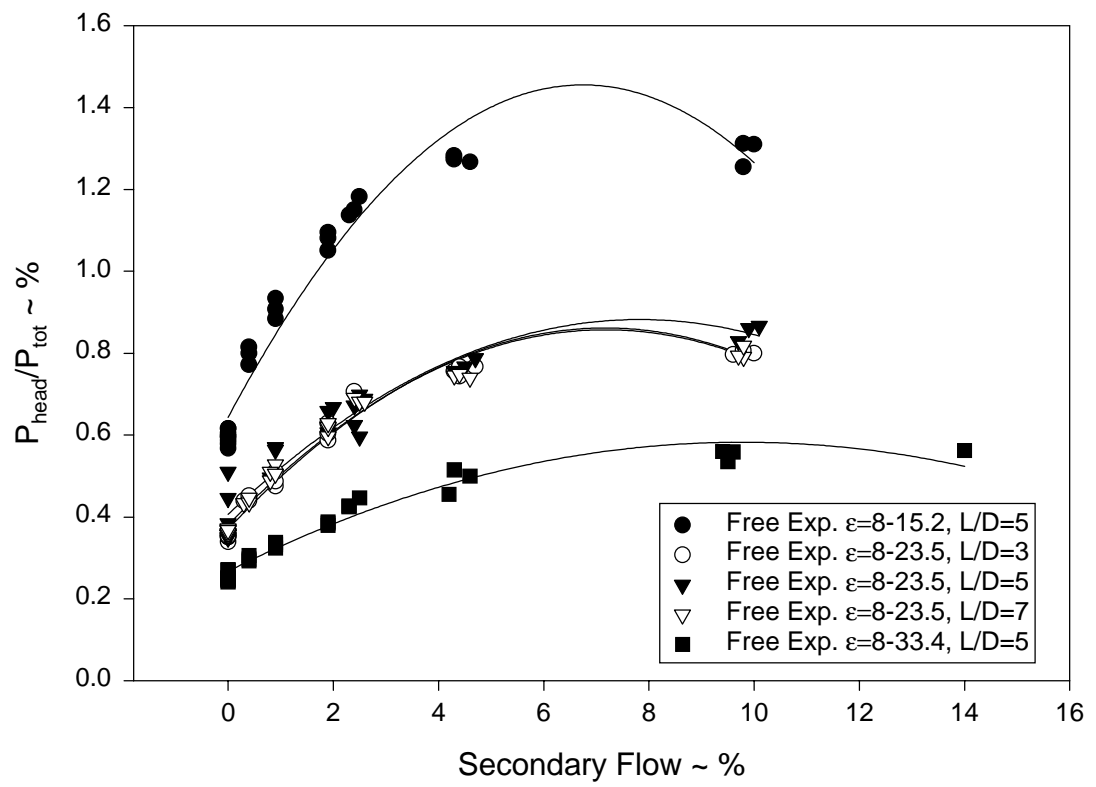


Figure 10. Ratio of duct head end pressure to rocket chamber total pressure.

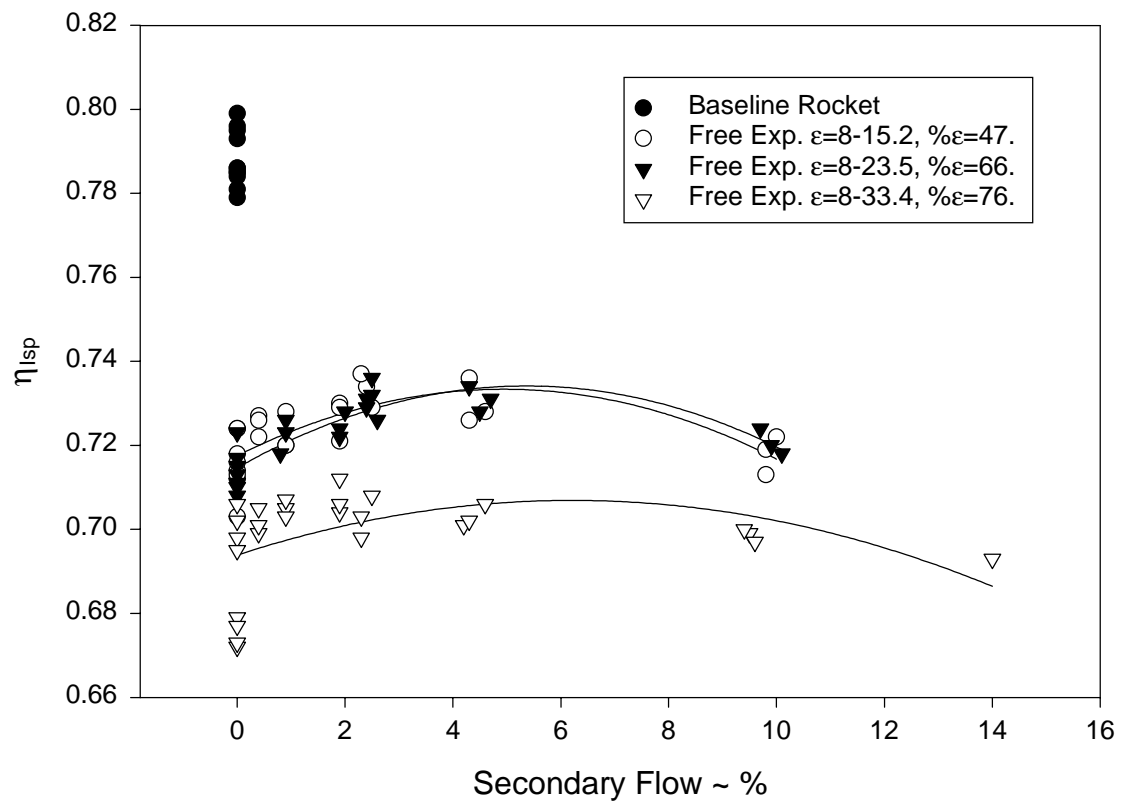


Figure 11. Specific impulse efficiency of rocket-in-a-duct for  $L/D=5$

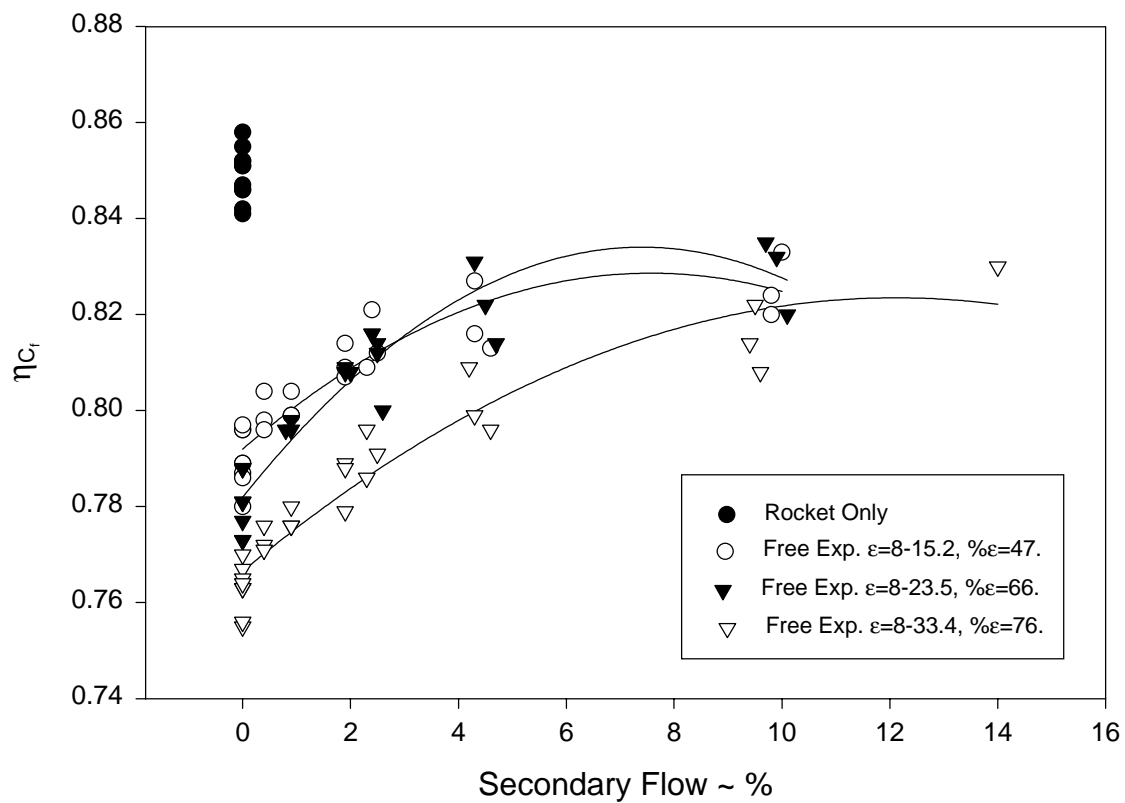


Figure 12. Thrust coefficient efficiency of rocket-in-a-duct for  $L/D=5$ .



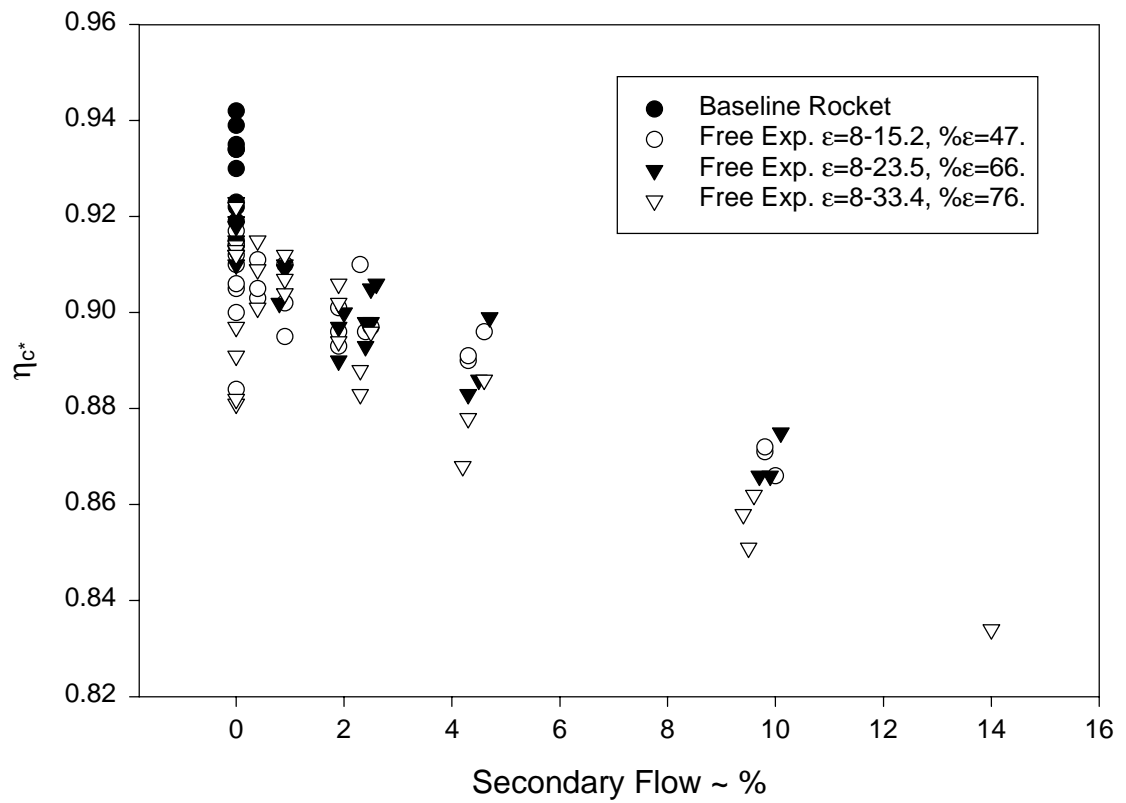


Figure 13. Characteristic velocity efficiency of rocket-in-a-duct for  $L/D=5$ .

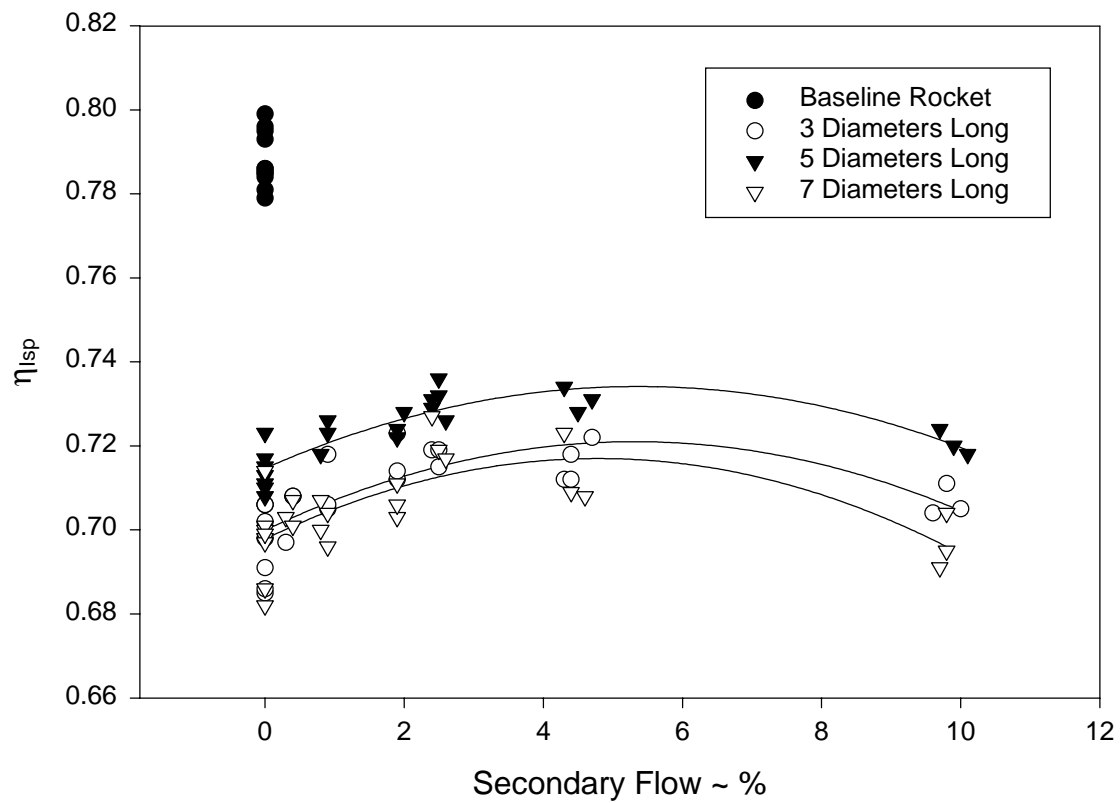


Figure 14. Specific impulse efficiency of rocket-in-a-duct with free expansion  $\epsilon=8-23.5$  as a function of percent secondary flow and length of duct

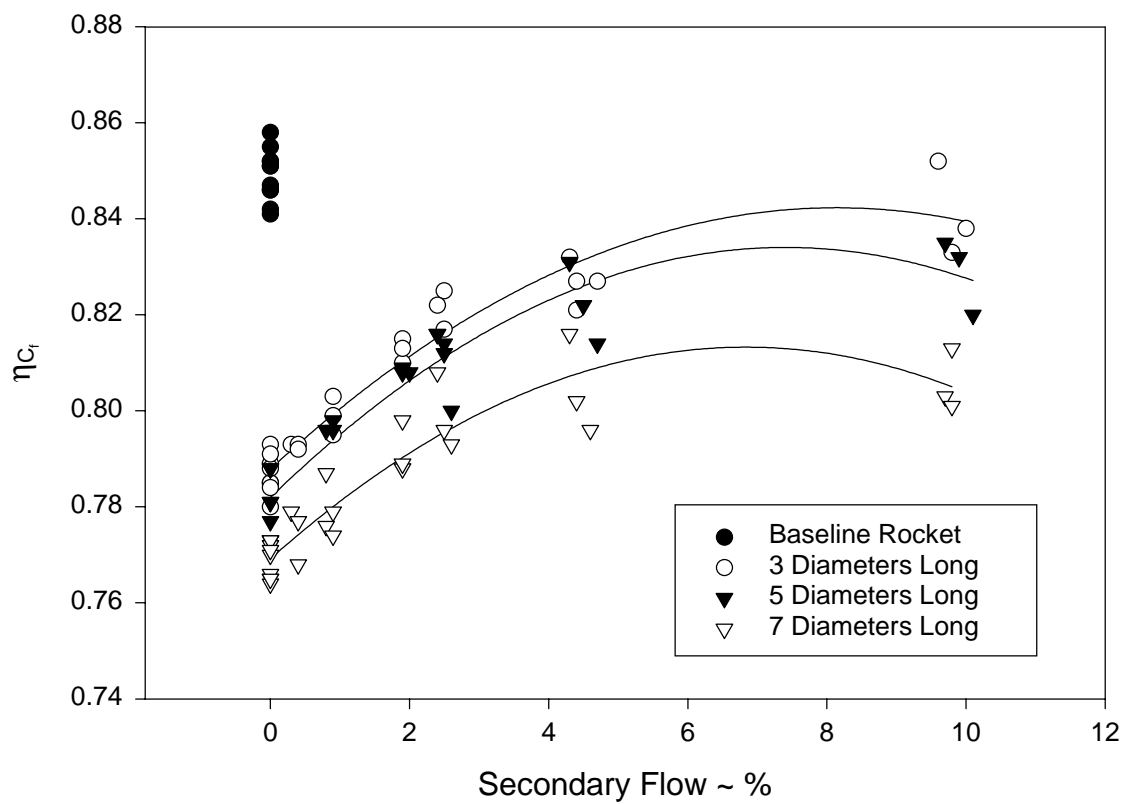


Figure 15. Thrust coefficient efficiency of rocket-in-a-duct with free expansion  $\epsilon=8-23.5$  as a function of percent secondary flow and length of duct

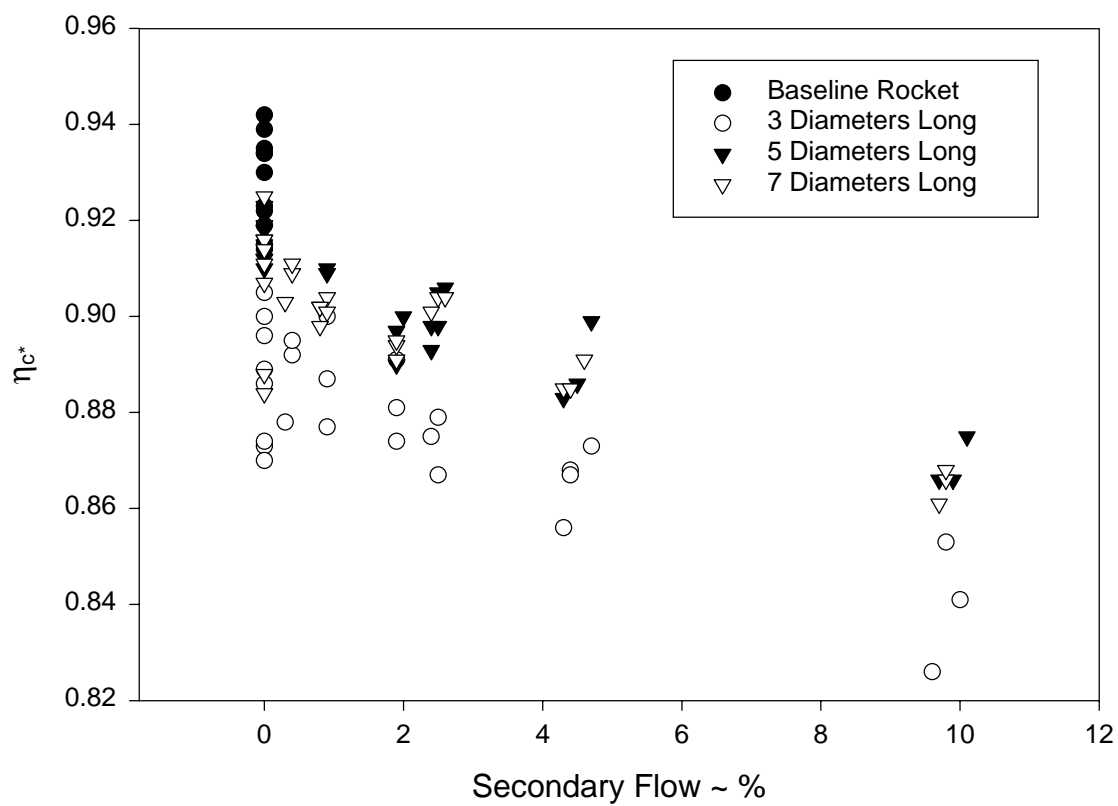


Figure 16. Characteristic velocity efficiency of rocket-in-a-duct with free expansion  $\epsilon=8-23.5$  as a function of percent secondary flow and length of duct

REPORT DOCUMENTATION PAGE			Form Approved OMB No. 0704-0188	
Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden, to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and Budget, Paperwork Reduction Project (0704-0188), Washington, DC 20503.				
1. AGENCY USE ONLY (Leave blank)	2. REPORT DATE October 1999	3. REPORT TYPE AND DATES COVERED Technical Memorandum		
4. TITLE AND SUBTITLE  Rocket-in-a-Duct Performance Analysis		5. FUNDING NUMBERS  WU-242-72-01-00		
6. AUTHOR(S)  Steven J. Schneider and Brian D. Reed				
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)  National Aeronautics and Space Administration John H. Glenn Research Center at Lewis Field Cleveland, Ohio 44135-3191		8. PERFORMING ORGANIZATION REPORT NUMBER  E-11918		
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)  National Aeronautics and Space Administration Washington, DC 20546-0001		10. SPONSORING/MONITORING AGENCY REPORT NUMBER  NASA TM-1999-209440 AIAA 99-2101		
11. SUPPLEMENTARY NOTES  Prepared for the 35th Joint Propulsion Conference and Exhibit cosponsored by the AIAA, ASME, SAE, and ASEE, Los Angeles, California, June 20-24, 1999. Responsible person, Steven J. Schneider, organization code 5430, (216) 977-7484.				
12a. DISTRIBUTION/AVAILABILITY STATEMENT  Unclassified - Unlimited Subject Category: 20  This publication is available from the NASA Center for AeroSpace Information, (301) 621-0390.			12b. DISTRIBUTION CODE	
13. ABSTRACT (Maximum 200 words)  An axisymmetric, 110 N class, rocket configured with a free expansion between the rocket nozzle and a surrounding duct was tested in an altitude simulation facility. The propellants were gaseous hydrogen and gaseous oxygen and the hardware consisted of a heat sink type copper rocket firing through copper ducts of various diameters and lengths. A secondary flow of nitrogen was introduced at the blind end of the duct to mix with the primary rocket mass flow in the duct. This flow was in the range of 0 to 10% of the primary massflow and its effect on nozzle performance was measured. The random measurement errors on thrust and massflow were within +/-1%. One dimensional equilibrium calculations were used to establish the possible theoretical performance of these rocket-in-a-duct nozzles. Although the scale of these tests was small, they simulated the relevant flow expansion physics at a modest experimental cost. Test results indicated that lower performance was obtained at higher free expansion area ratios and longer ducts, while, higher performance was obtained with the addition of secondary flow. There was a discernable peak in specific impulse efficiency at 4% secondary flow. The small scale of these tests resulted in low performance efficiencies, but prior numerical modeling of larger rocket-in-a-duct engines predicted performance that was comparable to that of optimized rocket nozzles. This remains to be proven in large-scale, rocket-in-a-duct tests.				
14. SUBJECT TERMS  Rocket-based combined cycle; Rocket nozzle performance; Experimental data			15. NUMBER OF PAGES 38	
			16. PRICE CODE A03	
17. SECURITY CLASSIFICATION OF REPORT  Unclassified	18. SECURITY CLASSIFICATION OF THIS PAGE  Unclassified	19. SECURITY CLASSIFICATION OF ABSTRACT  Unclassified	20. LIMITATION OF ABSTRACT	